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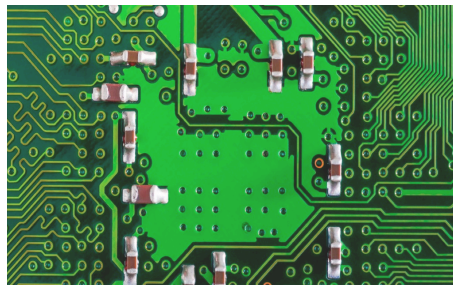
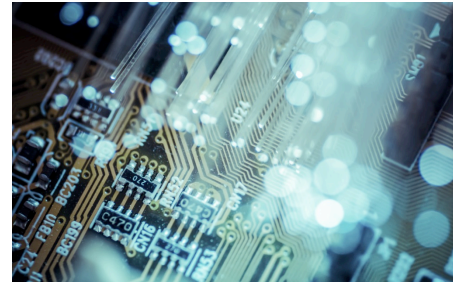
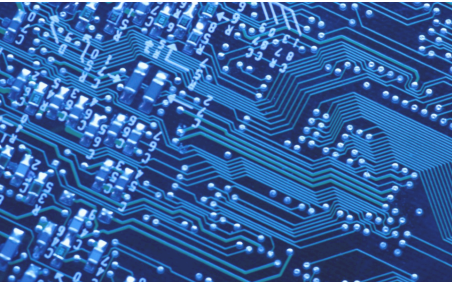


This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 671627



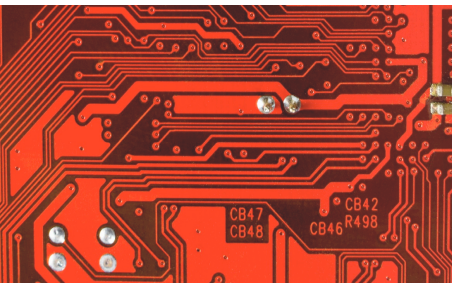
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Massively Parallel Computing for NWP and climate

Andreas Mueller
17.03.2017, Reading, UK



Energy-efficient Scalable Algorithms for Weather Prediction at Exascale





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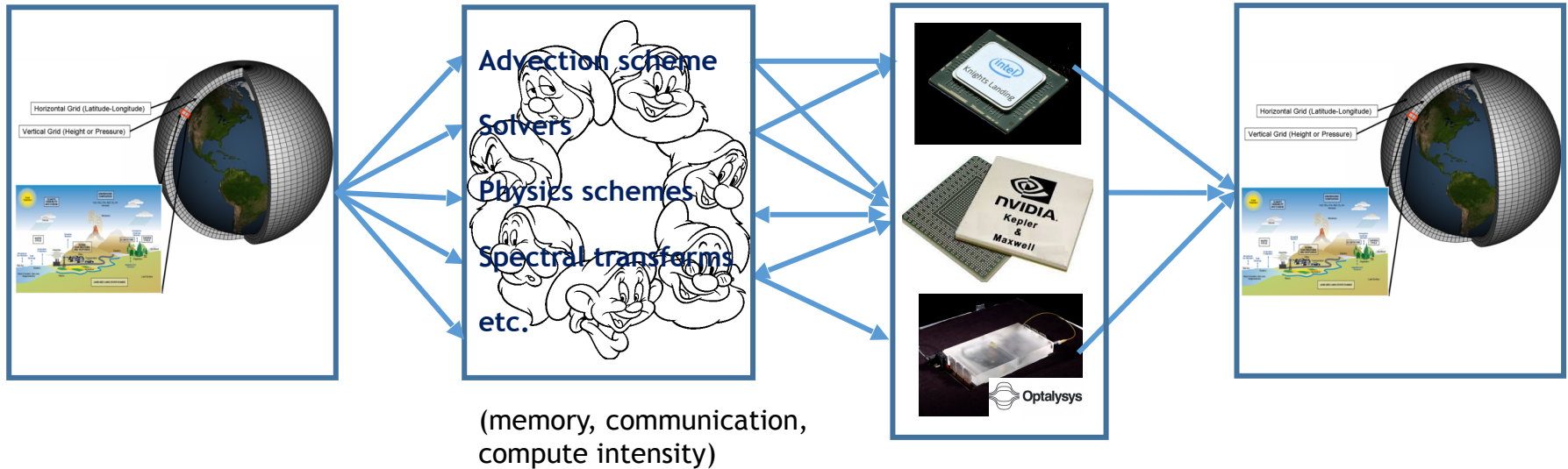
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Disassemble global ...
NWP model

Extract, redesign...
key components

Optimize for energy...
efficiency on new hardware

... Reassemble global
NWP model

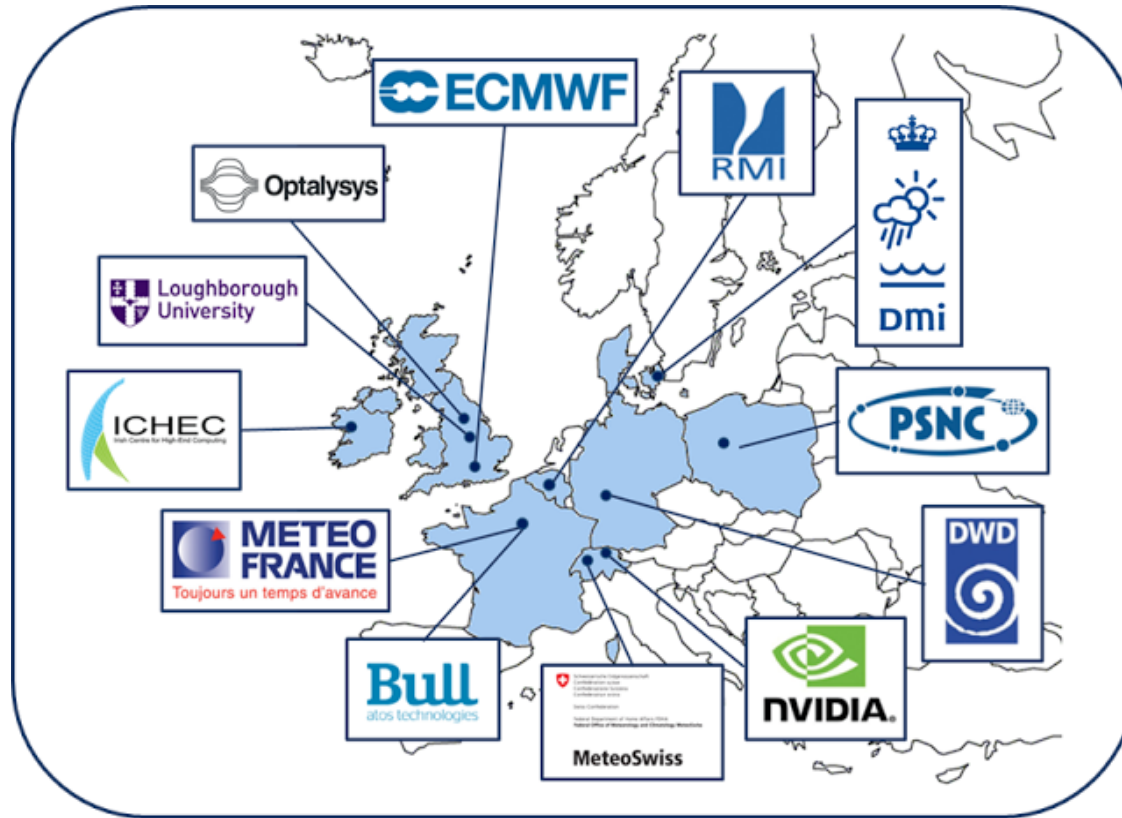




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Overview

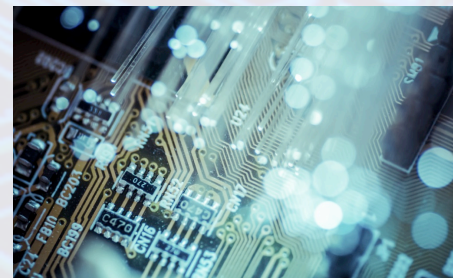
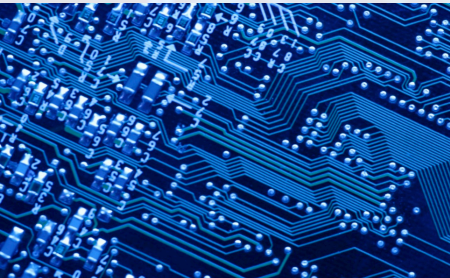
- Why do we as scientists need to know so much about computer science?
- What do we need to be aware of to write efficient code?
- How good are we?



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Why do we as scientists need to know so much about computer science?





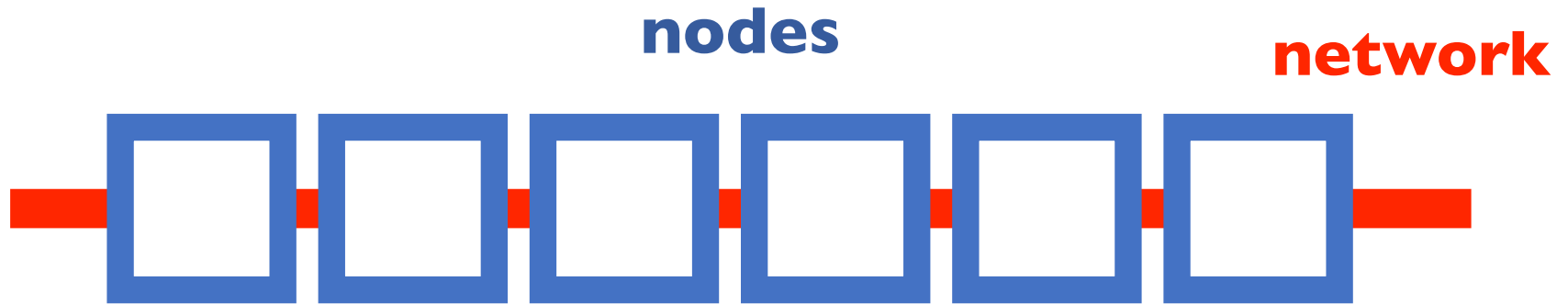
Why do we as scientists need to know so much about computer science?

- Excuse 1: let the computer scientists take care of it
- Response: computer scientists cannot do everything because they do not know about different numerical methods
- Excuse 2: just buy a faster computer if the code is not fast enough
- Response: we (and the environment) cannot afford wasting that much energy!

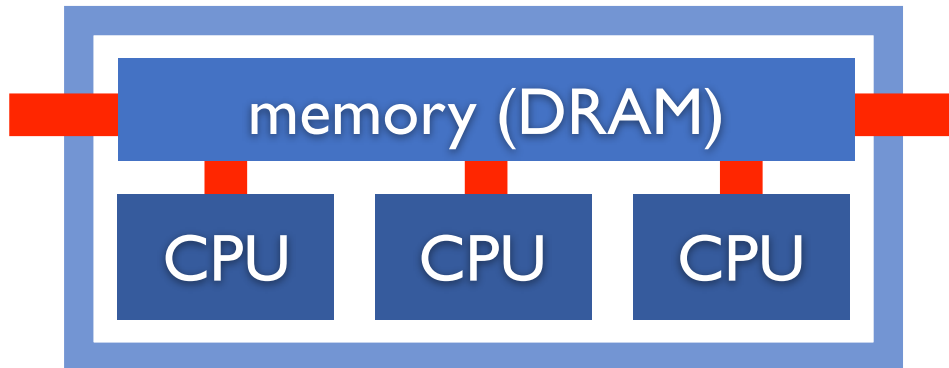
computer	electricity cost per year
ECMWF	~3 million £
fastest current supercomputer	~15 million \$
next generation (exascale)	~20 million \$



Supercomputer/Cluster



Node

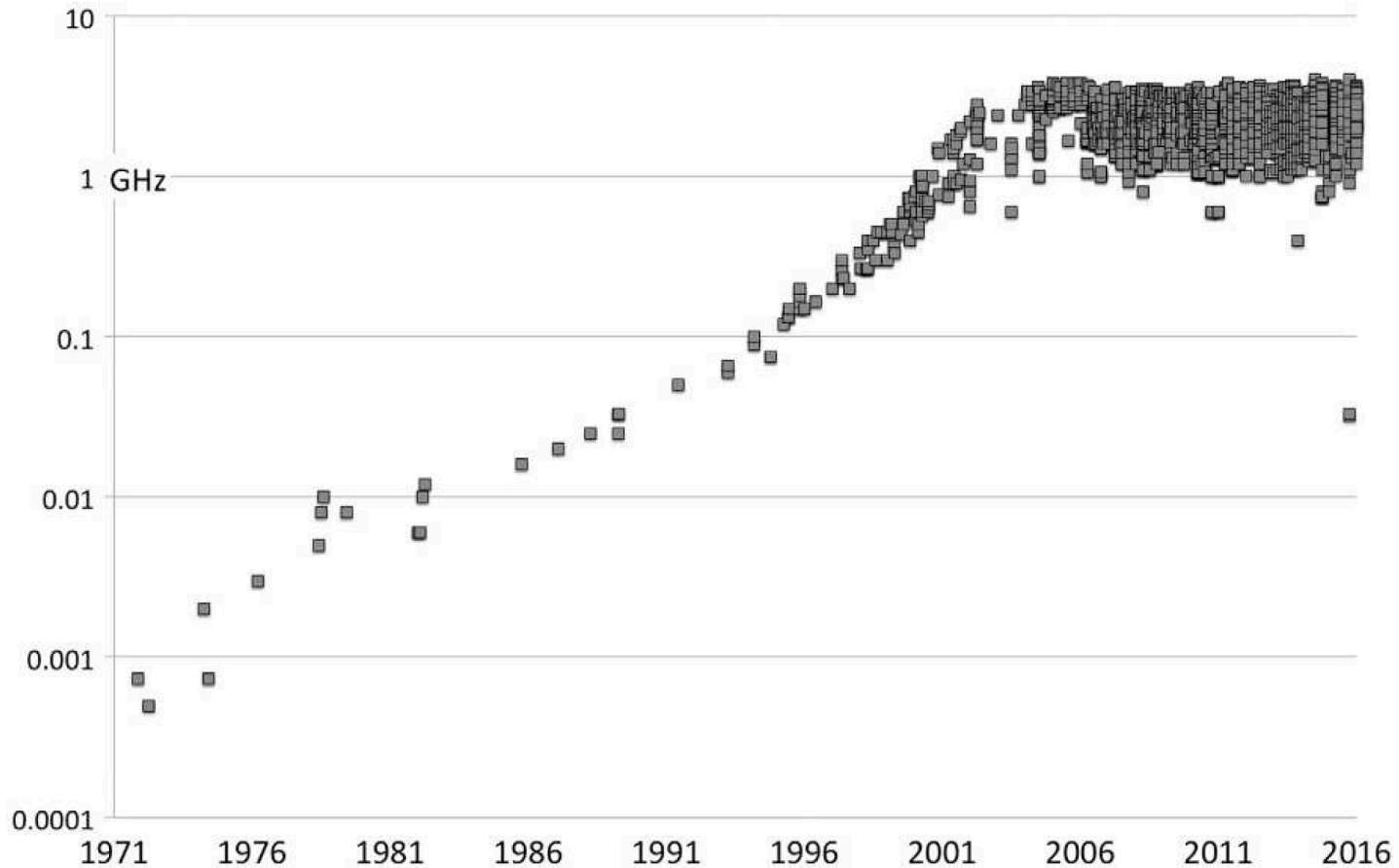


CPU

central processing unit;
does one instruction like
 $c=a+b$ per clock cycle

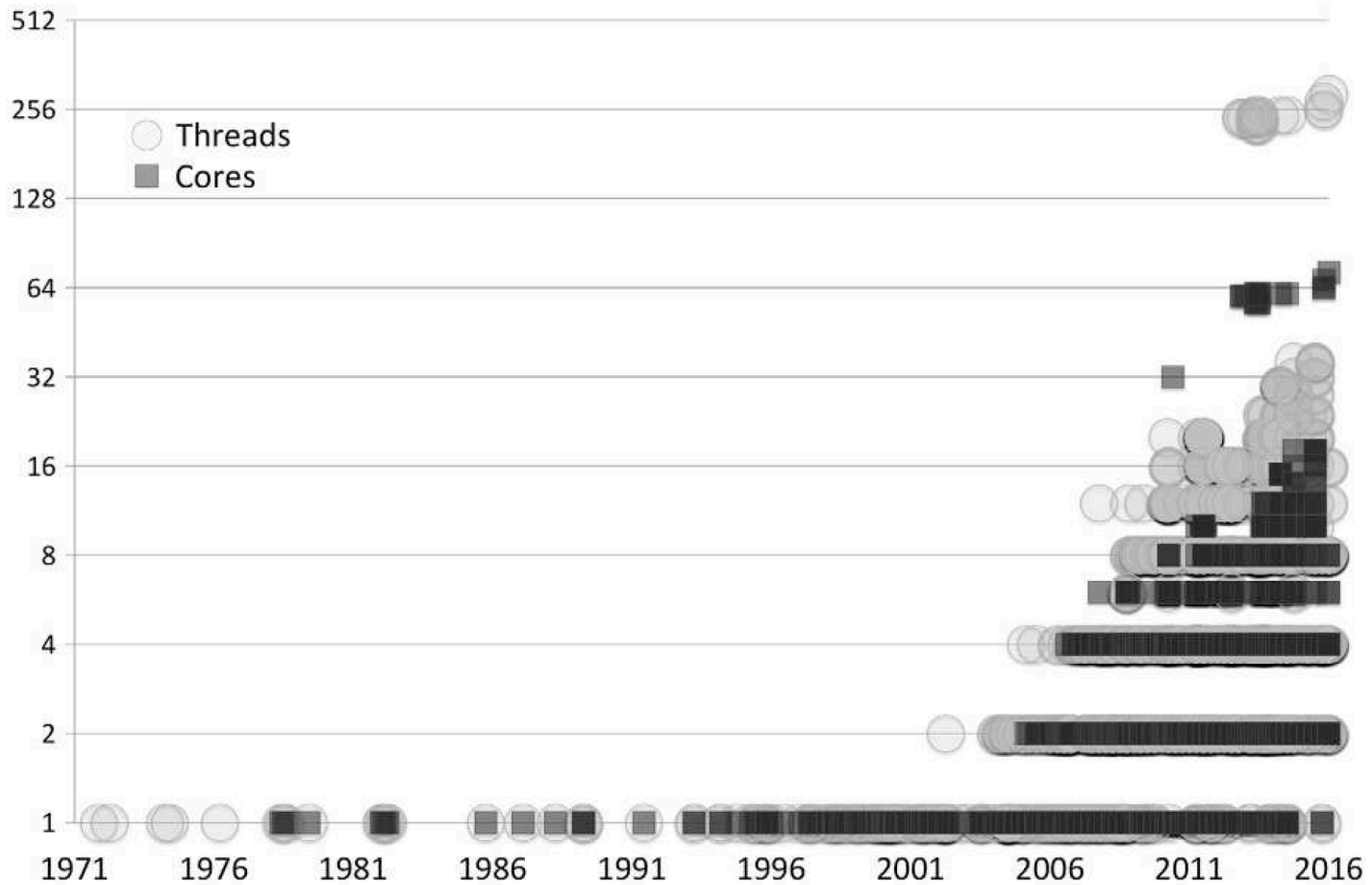


CPU clock rate over time





Number of cores per chip over time





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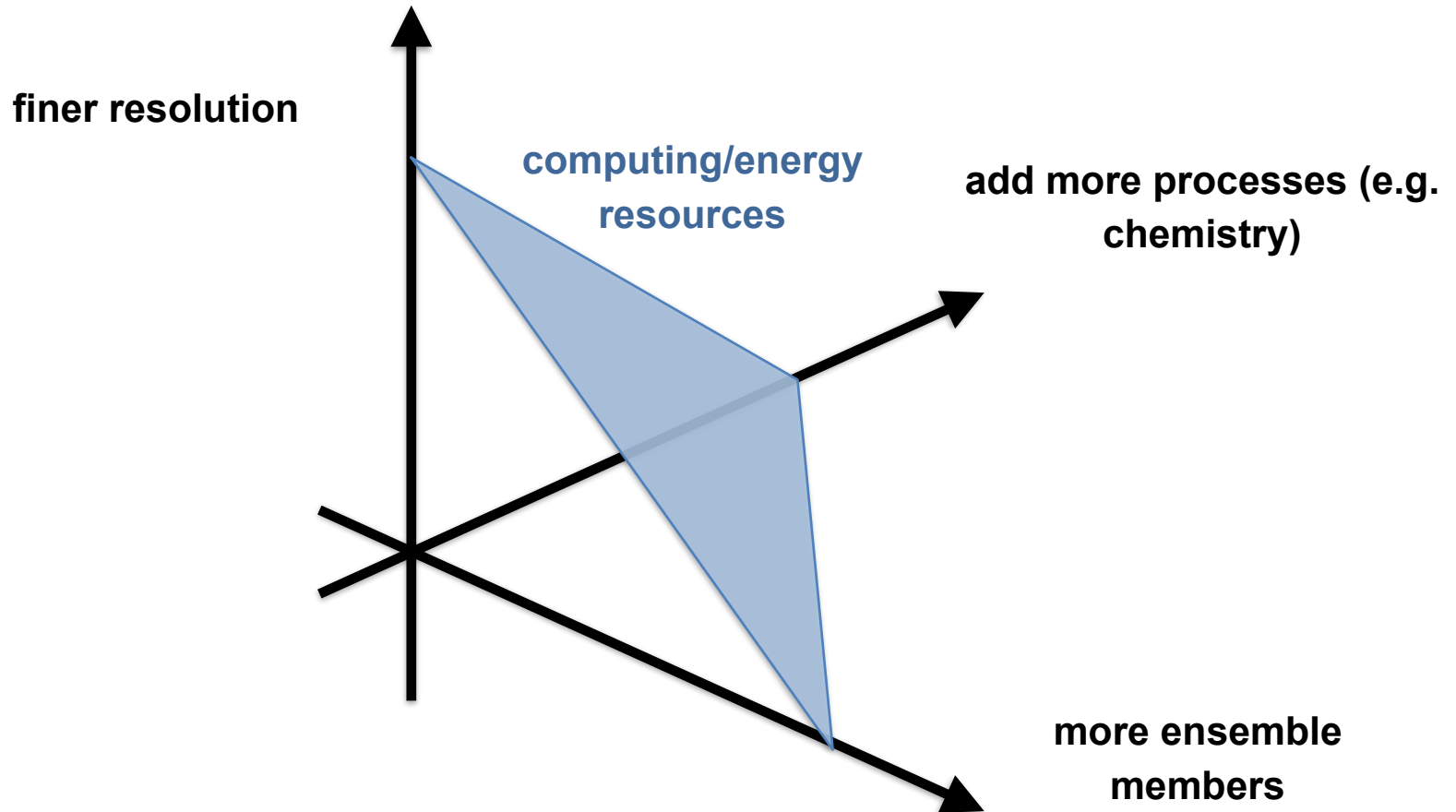
top500.org

Rank	Site	System	Cores	Rmax (TFlop/s)	Rpeak (TFlop/s)	Power (kW)
1	National Supercomputing Center in Wuxi China	Sunway TaihuLight - Sunway MPP, Sunway SW26010 260C 1.45GHz, Sunway NRCCP	10,649,600	93,014.6	125,435.9	15,371
2	National Super Computer Center in Guangzhou China	Tianhe-2 (MilkyWay-2) - TH-IVB-FEP Cluster, Intel Xeon E5-2692 12C 2.200GHz, TH Express-2, Intel Xeon Phi 31S1P NUDT	3,120,000	33,862.7	54,902.4	17,808
3	DOE/SC/Oak Ridge National Laboratory United States	Titan - Cray XK7 , Opteron 6274 16C 2.200GHz, Cray Gemini interconnect, NVIDIA K20x Cray Inc.	560,640	17,590.0	27,112.5	8,209
4	DOE/NNSA/LLNL United States	Sequoia - BlueGene/Q, Power BQC 16C 1.60 GHz, Custom IBM	1,572,864	17,173.2	20,132.7	7,890
5	DOE/SC/LBNL/NERSC United States	Cori - Cray XC40, Intel Xeon Phi 7250 68C 1.4GHz, Aries interconnect Cray Inc.	622,336	14,014.7	27,811.7	8,189
6	Joint Center for Advanced High Performance Computing Japan	Oakforest-PACS - PRIMERGY CX1640 M1, Intel Xeon Phi 7250 68C 1.4GHz, Intel Omni-Path Fujitsu	556,104	11,280.4	11,280.4	12,660
7	RIKEN Advanced Institute	K computer, SPARC64 VIIIfx 2.0GHz, Tofu	705,024	10,510.0	11,280.4	12,660





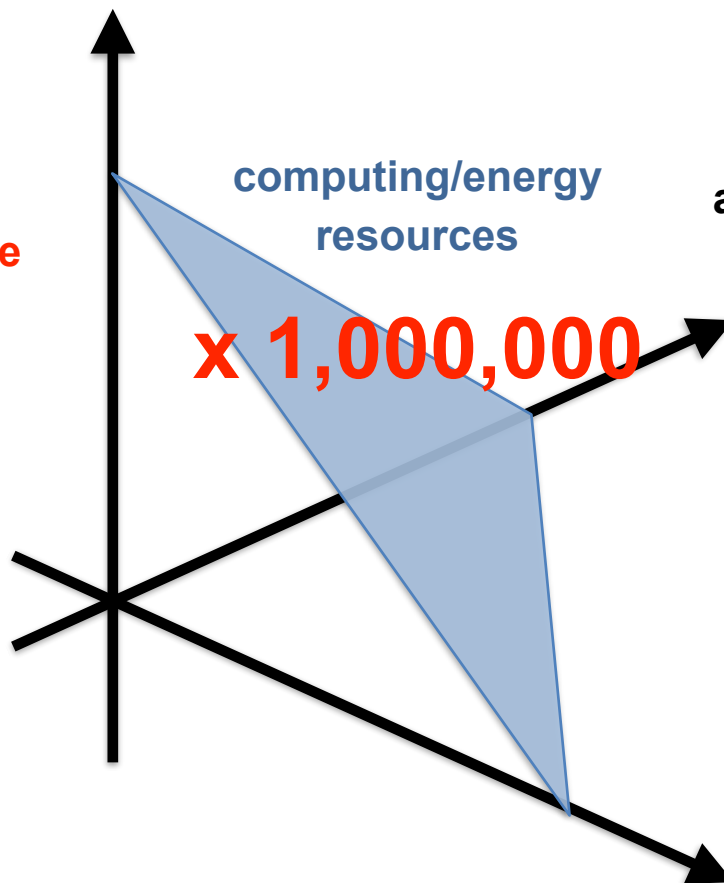
What next?





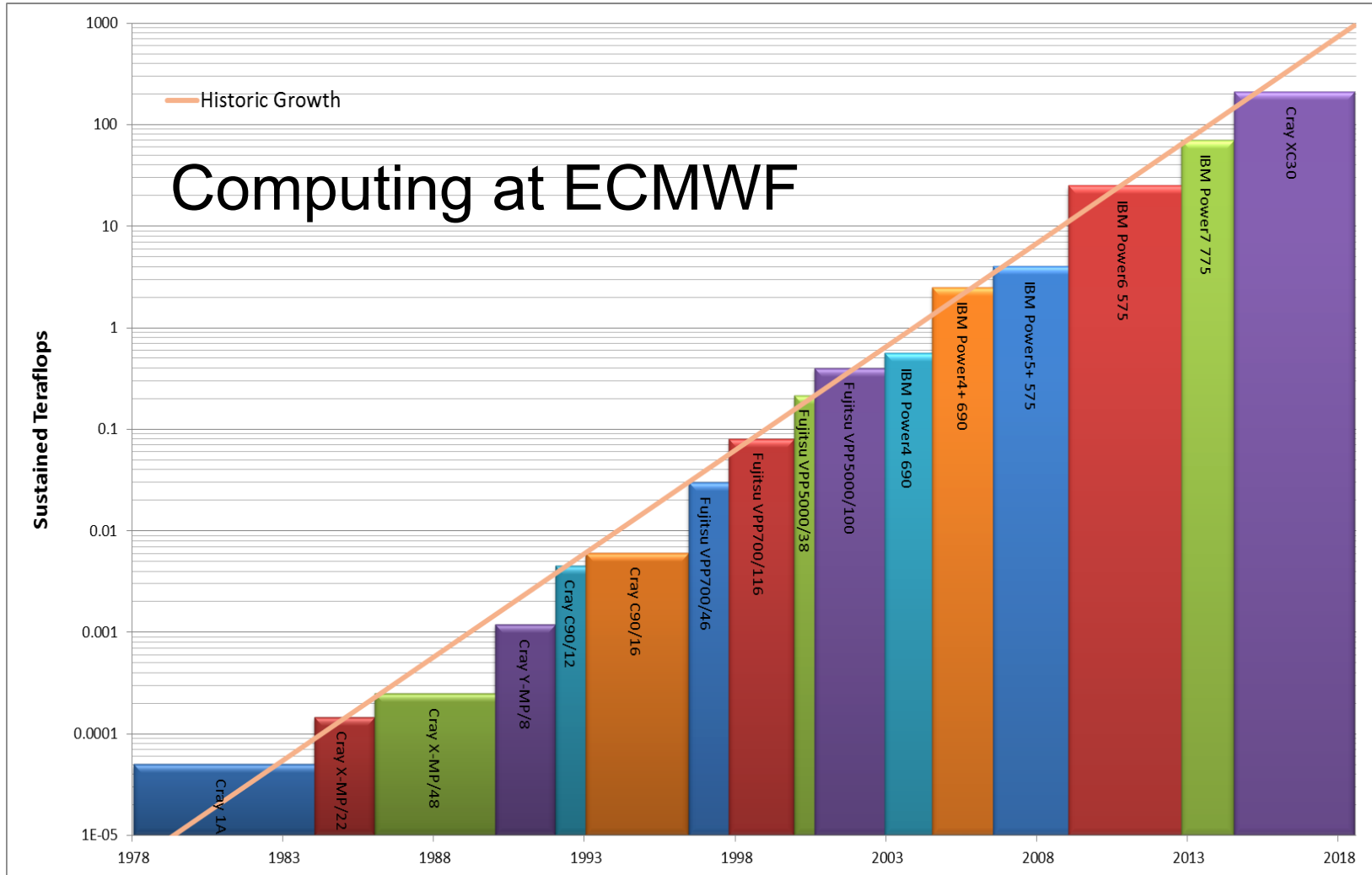
What next?

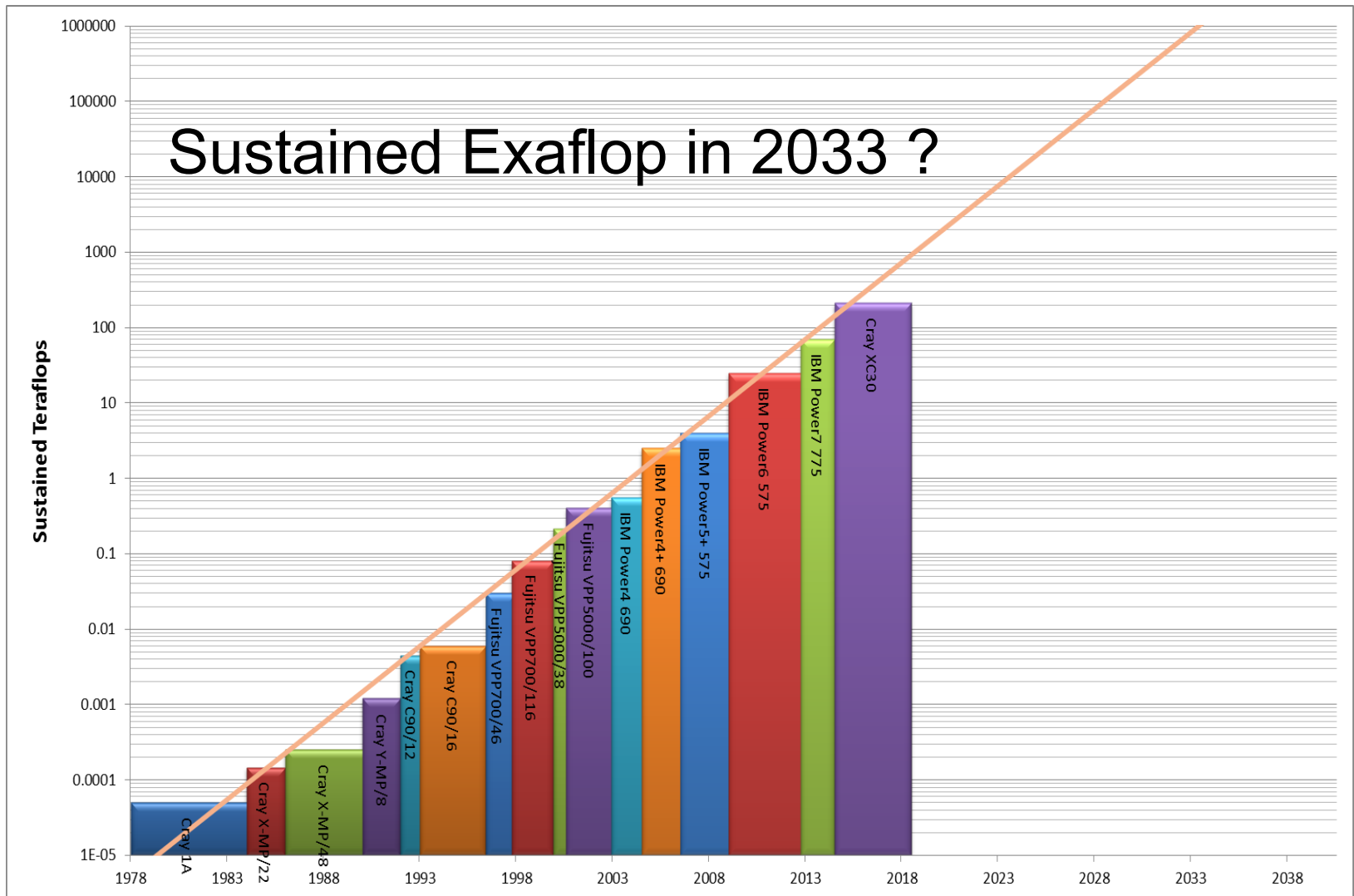
finer resolution
x 10 in each
direction and time
= 10,000



add more processes (e.g. chemistry)
x 10

more ensemble members
x 10





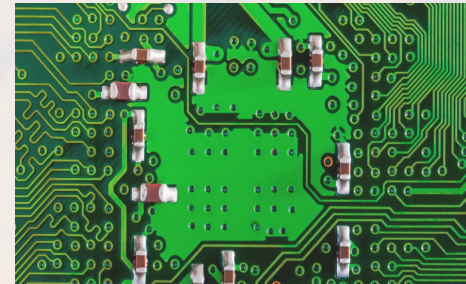
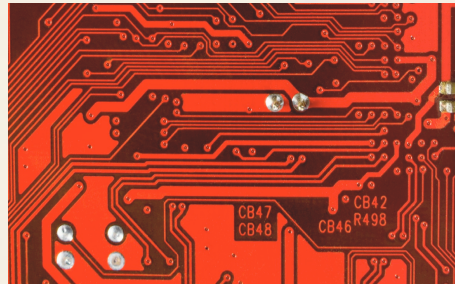
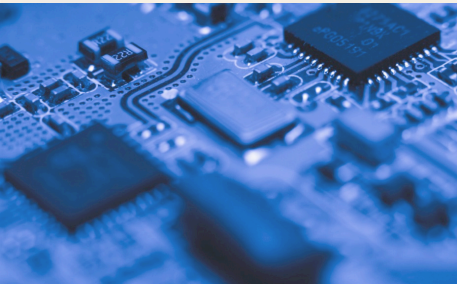


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What do we need to be aware of to write efficient code?

not covered: readability, portability, maintainability





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A graphic element for the ESCAPE logo, consisting of a blue grid pattern that fades into a white background.

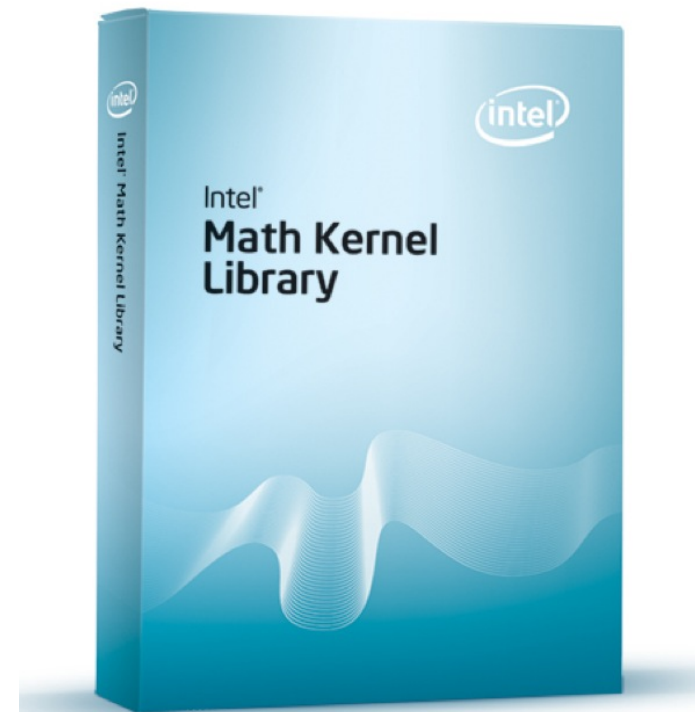
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List of recommendations



Libraries

- there are well optimised libraries for many tasks
- BLAS for vector-matrix product or matrix-matrix product (if matrices are large)
- Lapack for matrix factorisation (e.g. LU decomposition)
- some hardware vendors have special math libraries, e.g. MKL by Intel
- there are some cases in which libraries are fairly slow (e.g. BLAS with very small matrices)





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The logo for ESCAPE, with the word "ESCAPE" in a bold, blue, sans-serif font. The background of the logo is a blue grid pattern that fades into white.

List of recommendations

- **try if using libraries is fast enough**



Compiler optimisation

- compilers have optimisation flag `-On` (`O0`: no optimisation, `O3`: strong compiler optimisation)
- `O3` is usually much faster than `O2`, but it can also be slower than `O2`
- `O3` can produce completely wrong results!
- you can use different compiler flags for different files
- different compiler versions can have very different performance
- check compiler messages (Intel: `ifort -O2 -qopt-report=2 code.f90 -o program`)
- make sure that your code runs correctly with different compilers



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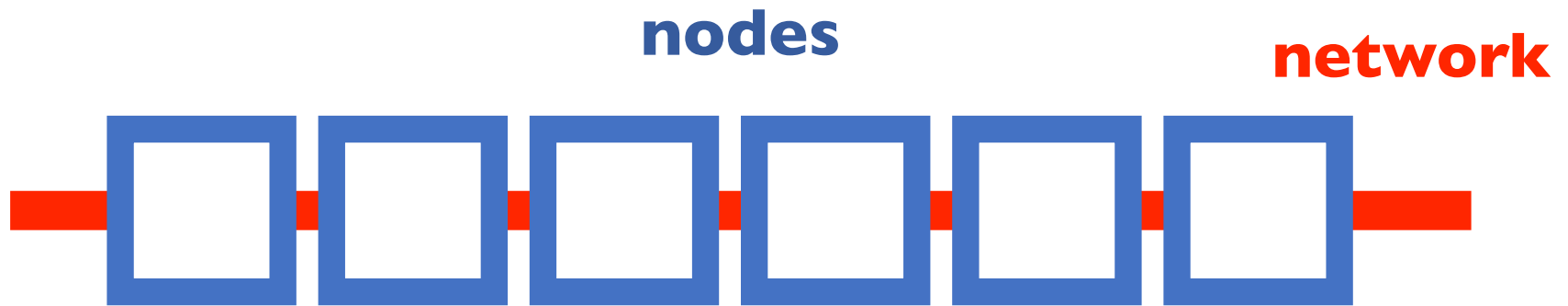
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List of recommendations

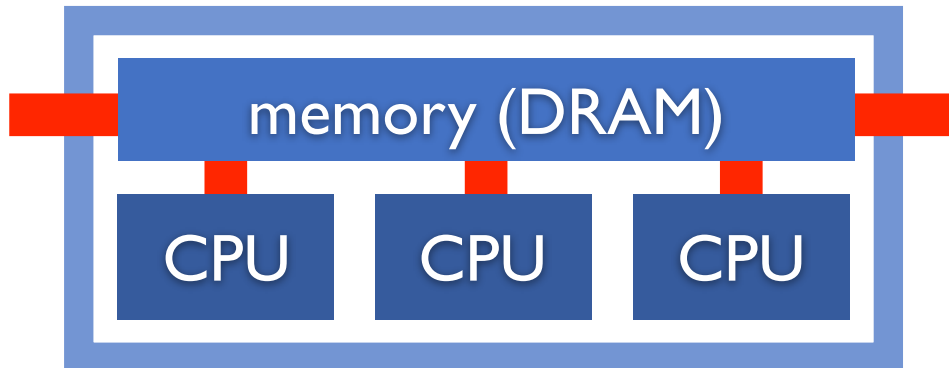
- try if using libraries is fast enough
- **try to use compiler optimisation (be careful!)**



Supercomputer/Cluster



Node



Bottlenecks

- network (connection between nodes)
- connection between DRAM and processor



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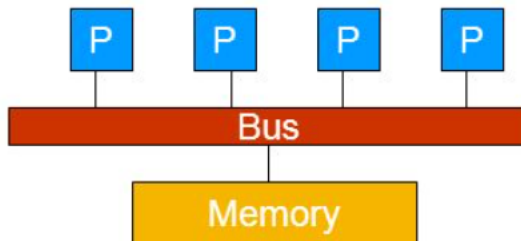
List of recommendations

- try if using libraries is fast enough
- try to use compiler optimisation (be careful!)
- **avoid unnecessary computation and communication**



Shared memory: OpenMP

- many threads of a process run on a single node
- all threads can access the same data
- data may be physically distributed, but logically shared



without OpenMP:

```
real, dimension(N) :: a,b
integer :: i,N
do i=1,N
  a(i) = a(i) + b(i)
end do
```

with OpenMP:

```
real, dimension(N) :: a,b
integer :: i,N
!$omp parallel do private(i)
do i=1,N
  a(i) = a(i) + b(i)
end do
!$omp end parallel do
```




Shared memory: OpenMP

faster for bigger codes:

```
real, dimension(N) :: a,b
integer :: i, N, iStart, iEnd,
    myid, numthreads
!$omp parallel private(i,iStart,iEnd)
myid = omp_get_thread_num()
numthreads = omp_get_num_threads()
iStart = ...
iEnd = ...
do i=iStart,iEnd
    a(i) = a(i) + b(i)
end do
!$omp end parallel
```

without OpenMP:

```
real, dimension(N) :: a,b
integer :: i,N
do i=1,N
    a(i) = a(i) + b(i)
end do
```

with OpenMP:

```
real, dimension(N) :: a,b
integer :: i,N
!$omp parallel do private(i)
do i=1,N
    a(i) = a(i) + b(i)
end do
!$omp end parallel do
```



List of recommendations

- try if using libraries is fast enough
- try to use compiler optimisation (be careful!)
- avoid unnecessary computation and communication
- **decide yourself how to parallelise your code**



Shared memory: OpenMP

Example 2: race conditions

without OpenMP:

```
real, dimension(N) :: a
real :: sum
integer :: i,N
do i=1,N
    sum = sum + a(i)
end do
```

with OpenMP (wrong!):

```
real, dimension(N) :: a
real :: sum
integer :: i,N
!$omp parallel do private(i)
do i=1,N
    sum = sum + a(i)
end do
!$omp end parallel do
```

working, but slow:

```
real, dimension(N) :: a
real :: sum
!$omp parallel do private(i)
do i=1,N
    !$omp atomic
    sum = sum + a(i)
end do
!$omp end parallel do
```

faster:

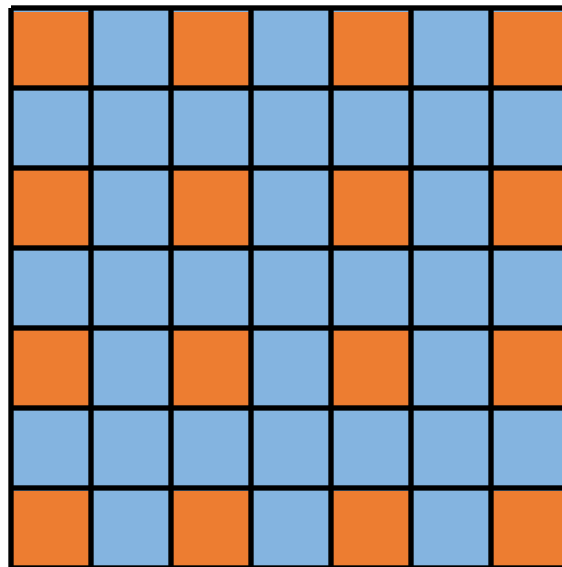
```
real, dimension(N) :: a
real :: sum
!$omp parallel do private(i)
    reduction (+: sum )
do i=1,N
    sum = sum + a(i)
end do
!$omp end parallel do
```



Shared memory: OpenMP

Example 2: race conditions

best: arrange work such that different threads work on different data



example: spectral
element, start with
orange (non-
adjacent) elements



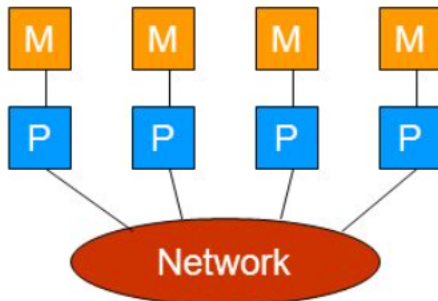
List of recommendations

- try if using libraries is fast enough
- try to use compiler optimisation (be careful!)
- avoid unnecessary computation and communication
- decide yourself how to parallelise your code
- **let the threads do work that does not affect others**



Distributed memory: MPI

- many processes run on multiple nodes
- process can access only data on the node it is running
- use communication library MPI (Message Passing Interface) to access data on other nodes

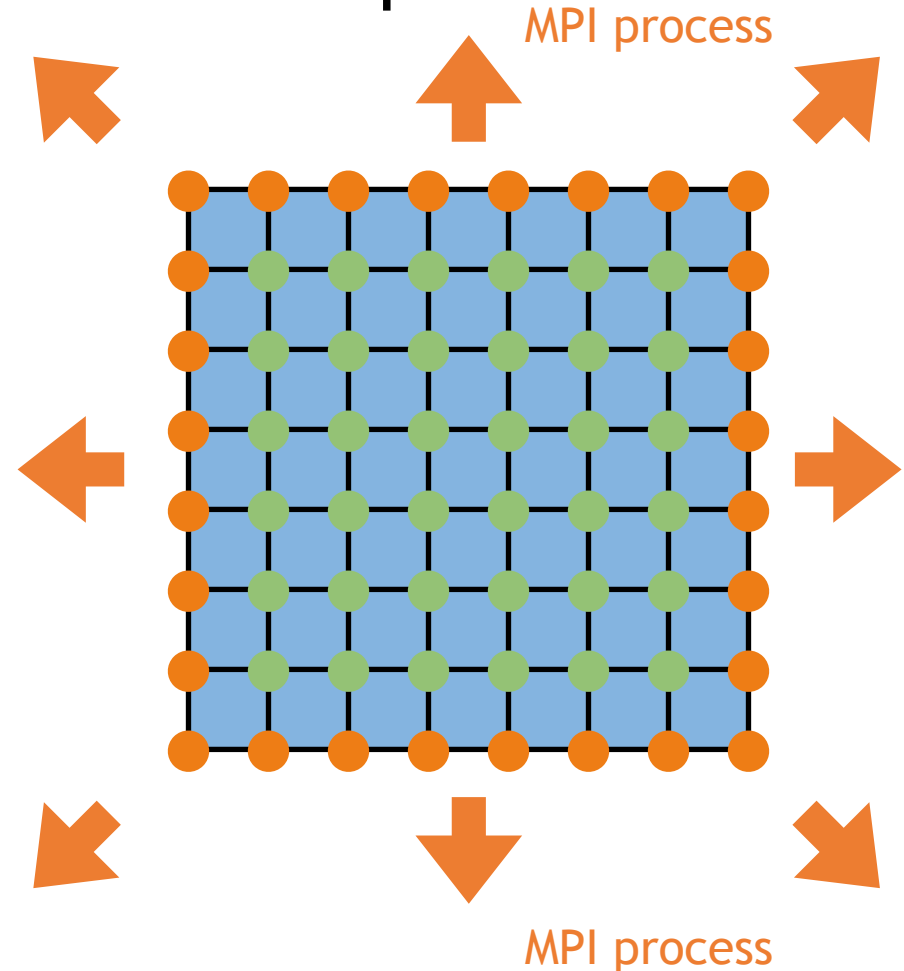


```
integer :: len, destination, tag, nreq
comm = mpi_comm_world
call mpi_init(ierr)
call mpi_comm_rank(comm, myid, ierr)
call mpi_comm_size(comm, numproc, ierr)
nreq = 0
...
do i=1,N ! loop over processors with which we
        ! want to communicate
    destination = ...
    nreq = nreq + 1
    call mpi_irecv(recvdata, len, mpi_real,
                  destination, tag, comm, request(nreq),
                  ierr)
    nreq = nreq + 1
    call mpi_isend(senddata, len, mpi_real,
                  destination, tag, comm, request(nreq),
                  ierr)
end do
... do some work ...
call mpi_waitall(nreq, request, status, ierr)
call mpi_finalize(ierr)
```



Overlap communication and computation

- Example: grid point method with only next neighbour communication:
 - compute values along processor boundaries first (orange) and send result to neighbours
 - compute interior points while the data is on its way (green)
- try to reduce the physical distance that data needs to travel (difficult)





List of recommendations

- try if using libraries is fast enough
- try to use compiler optimisation (be careful!)
- avoid unnecessary computation and communication
- decide yourself how to parallelise your code
- let the threads do work that does not affect others
- **overlap computation and communication**



Use data once per time-step

bad example:

```
real, dimension(N) :: a,b
real :: sum
integer :: i,N
sum = 0.0
a = 0.0
b = 0.0
do i=1,N
  b(i) = i
end do
do i=1,N
  a(i) = a(i) + b(i)
end do
do i=1,N
  sum = sum + a(i)
end do
print*,sum
```

good:

```
real, dimension(N) :: a,b
real :: sum
integer :: i,N
sum = 0.0
do i=1,N
  a(i) = 0.0
  b(i) = i
  a(i) = a(i) + b(i)
  sum = sum + a(i)
end do
print*,sum
```



List of recommendations

- try if using libraries is fast enough
- try to use compiler optimisation (be careful!)
- avoid unnecessary computation and communication
- decide yourself how to parallelise your code
- let the threads do work that does not affect others
- overlap computation and communication
- **use data only once per time-step**



Contiguous memory access

double precision
floating point number (64bit) memory



cache line
(often 128 Bytes)



store data in the order in which you need it
and use it in this order!

Fortran (column major order):

```
real, dimension(N,M) :: a,b
integer :: i,j,N,M
do j=1,M
  do i=1,N
    a(i,j) = a(i,j) + b(i,j)
    ! fast index should be i
  end do
end do
```

C (row major order):

```
int i,j,N,M;
for (i=0; i<N; i++) {
  for (j=0; j<M; j++) {
    a[i][j] = a[i][j] + b[i][j]
    // fast index should be j
  }
}
```

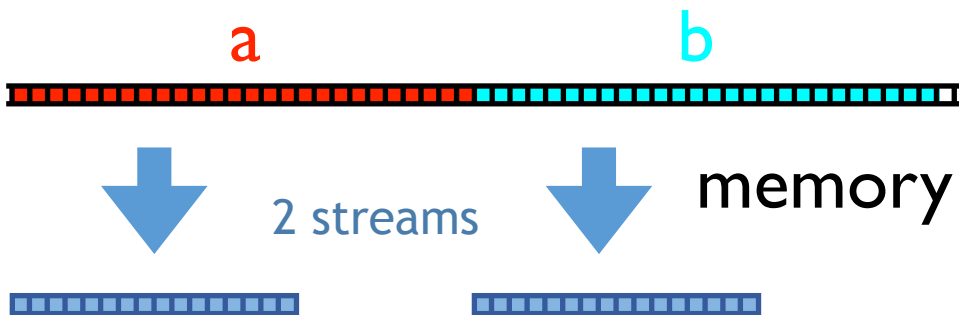


Contiguous memory access

best: one stream of data (good for prefetching)

example:

```
real, dimension(N) :: a,b  
integer :: i,N  
do i=1,N  
  a(i) = a(i) + b(i) } 2 streams  
end do
```





Contiguous memory access

best: one stream of data (good for prefetching)

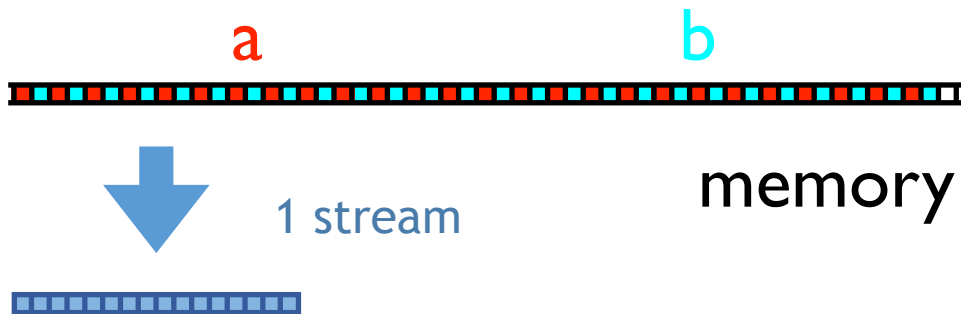
example:

```

real, dimension(N) :: a,b
integer :: i,N
do i=1,N
  a(i) = a(i) + b(i)
end do

```

} 2 streams



better for prefetching:

```

real, dimension(N) :: a,b
real, dimension(2*N) :: c
integer :: i,N
do i=1,N
  c(2*i) = a(i)
  c(2*i-1) = b(i)
end do
do i=1,2*N,2
  c(i) = c(i) + c(i-1)
end do
do i=1,N
  a(i) = c(2*i)
end do

```

} 1 stream

efficient, if data needs to be rearranged only at beginning and end of simulation!

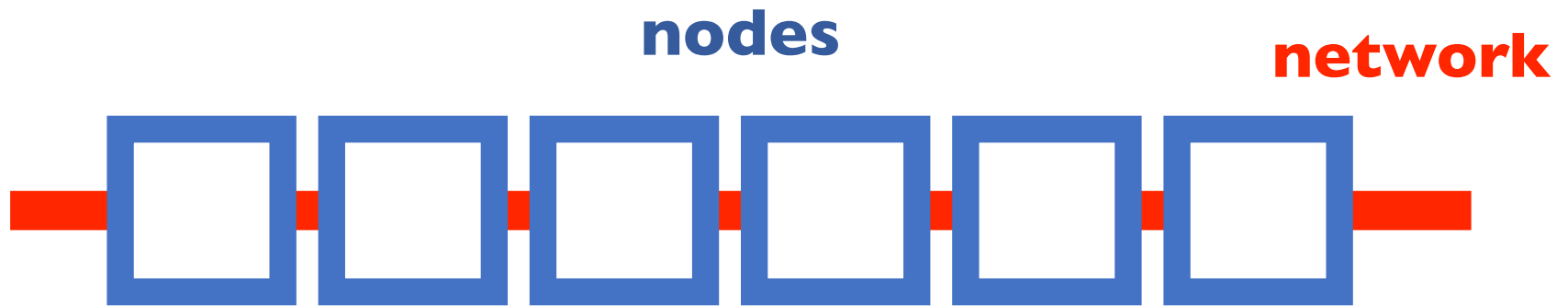


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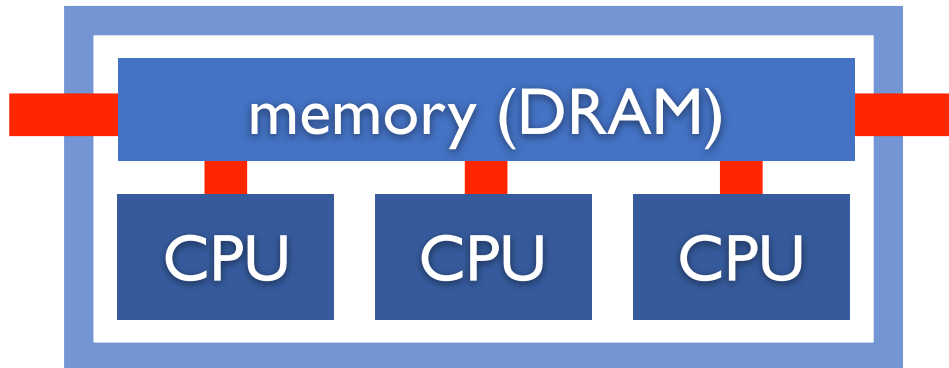
- try if using libraries is fast enough
- try to use compiler optimisation (be careful!)
- avoid unnecessary computation and communication
- decide yourself how to parallelise your code
- let the threads do work that does not affect others
- overlap computation and communication
- use data only once per time-step
- **contiguous memory access**



Supercomputer/Cluster



Node

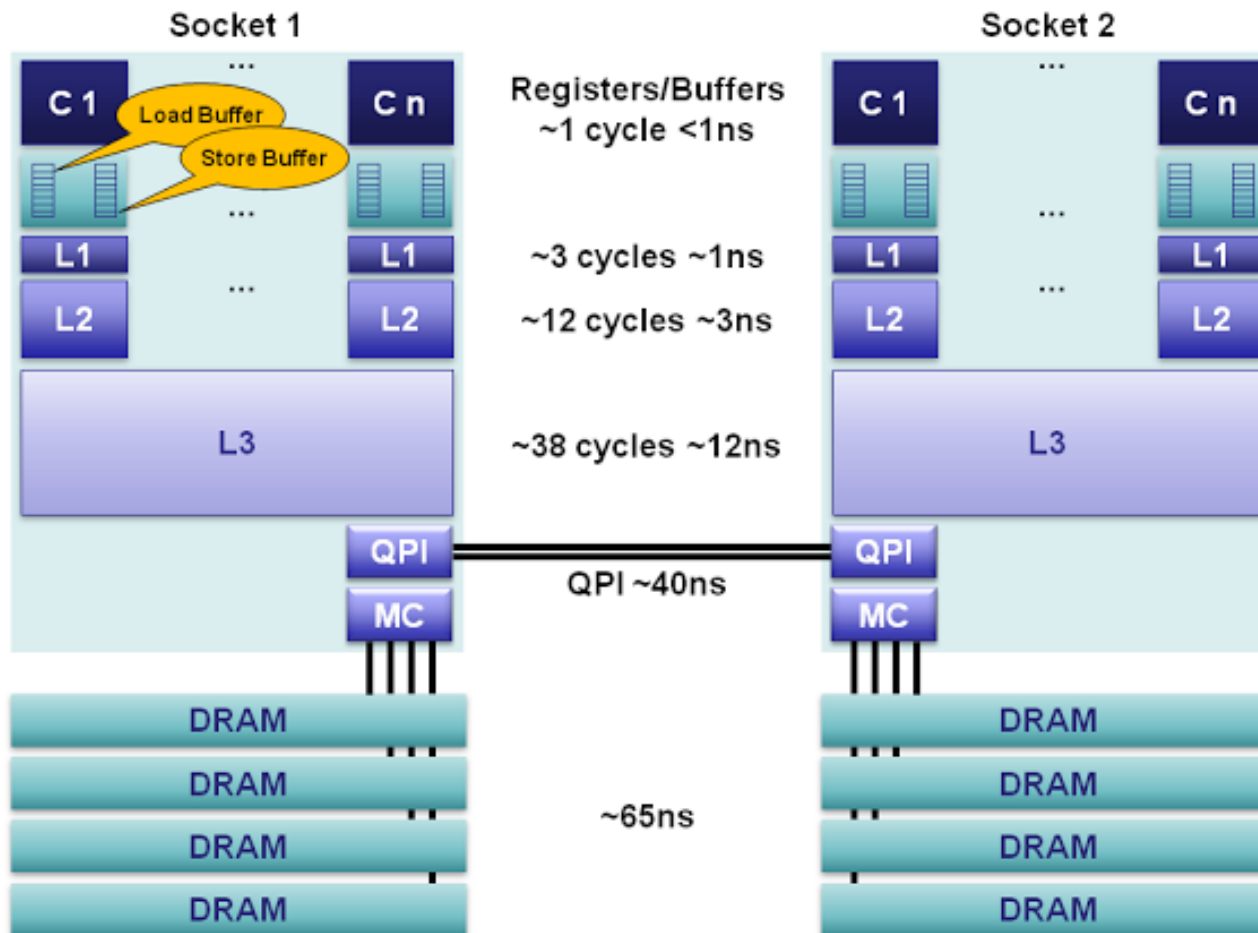


CPU

central processing unit;
does one instruction like
 $c=a+b$ per clock cycle

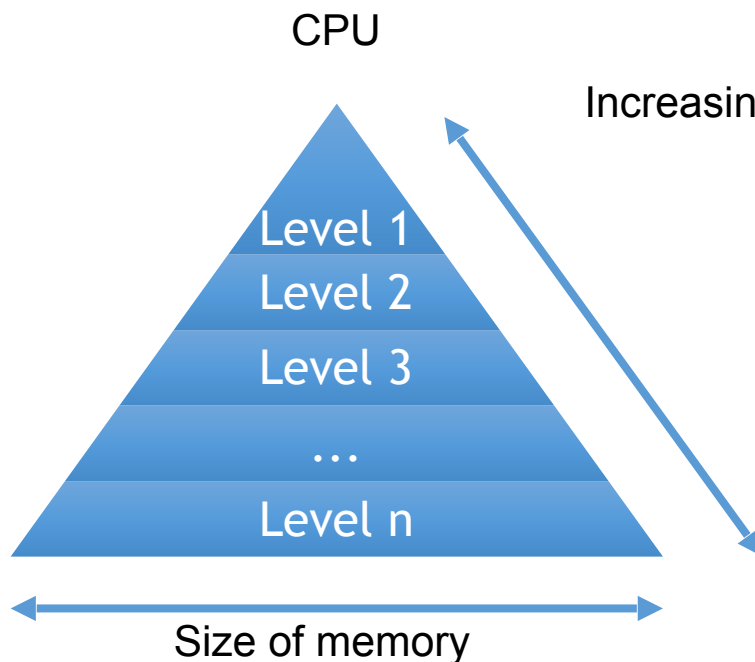


Memory hierarchy inside one node





Cache



Example:

L1: 32 kB, latency 3 cycles

L2: 256 kB, latency 10 cycles

L3: 8MB, latency 40 cycles

DRAM: 16GB, latency 200 cycles

DISK: 1TB, latency 1.000.000 cycles

Cache hit – data found in cache

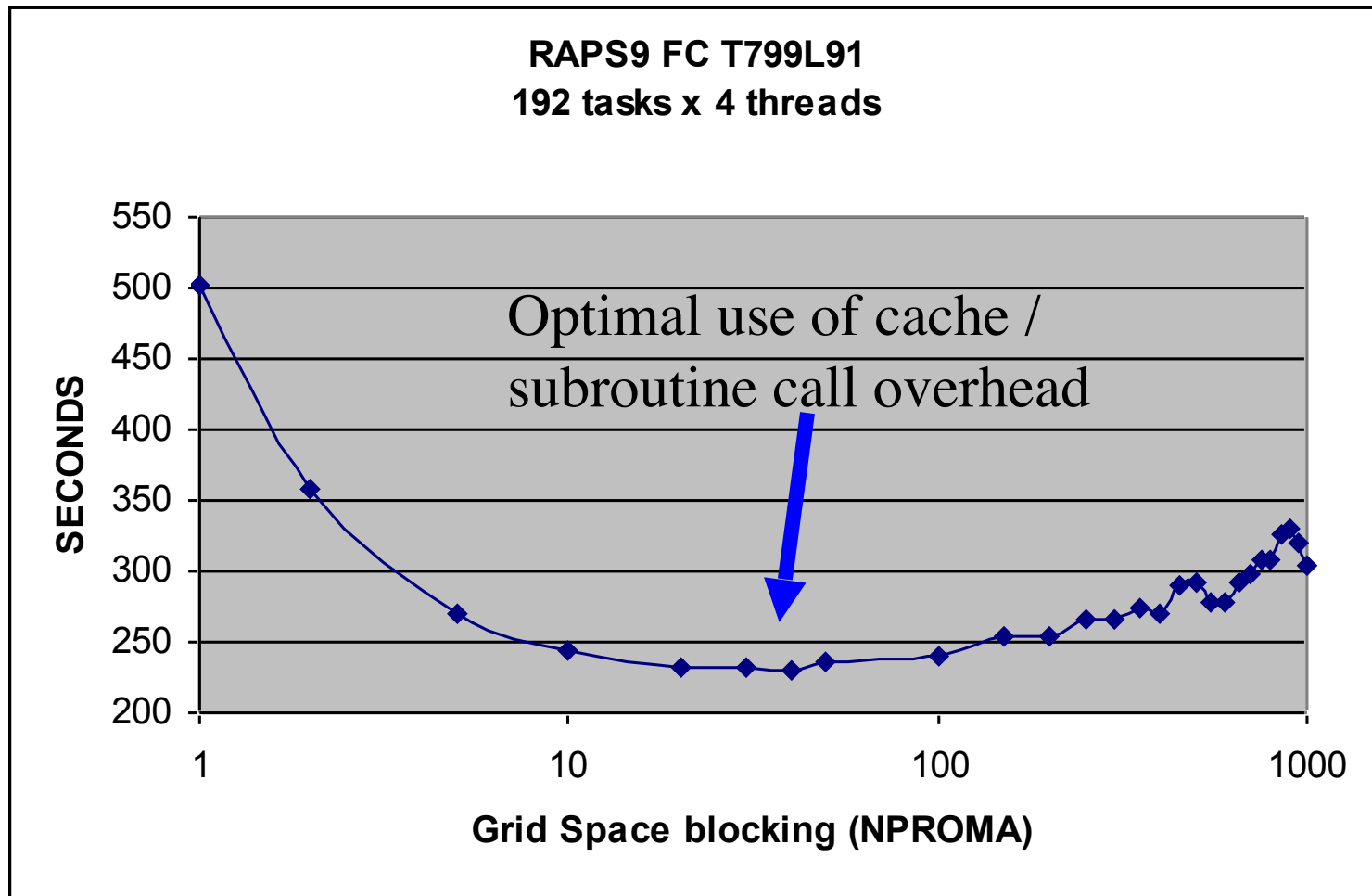
Cache miss – data not found in cache, thus must be copied from lower memory level

Capacity miss – cache runs out of space for new data

Conflict miss – more that one item is mapped to the same location in cache



IFS: divide work into blocks with length NPROMA



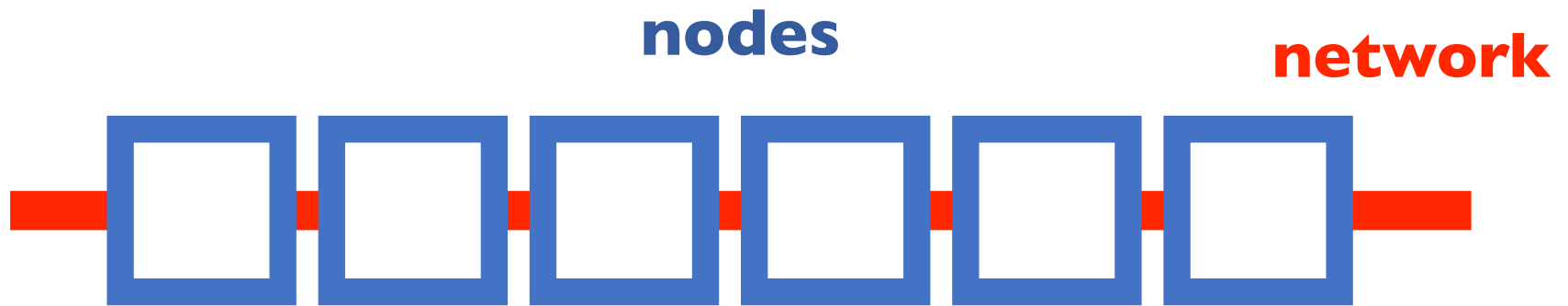


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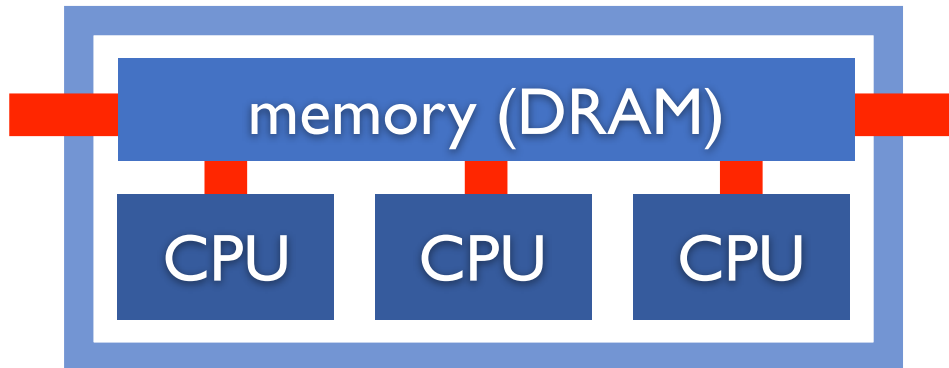
- try if using libraries is fast enough
- try to use compiler optimisation (be careful!)
- avoid unnecessary computation and communication
- decide yourself how to parallelise your code
- let the threads do work that does not affect others
- overlap computation and communication
- use data only once per time-step
- contiguous memory access
- **try to fit data into cache**



Supercomputer/Cluster



Node



Bottlenecks

- network (connection between nodes)
- connection between DRAM and processor



Fast and slow operations

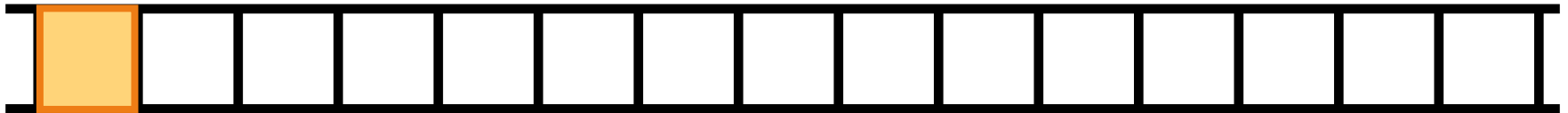
- In terms of cost
 - Fast and inexpensive: add, multiply, sub, fma (fused multiply add)
 - Medium: divide, modulus, sqrt
 - Slow: power, trigonometric functions
-
- try linear algebra (BLAS, LAPACK) and math libraries (Intel MKL)



Vectorisation

double precision
floating point number (64bit)

memory

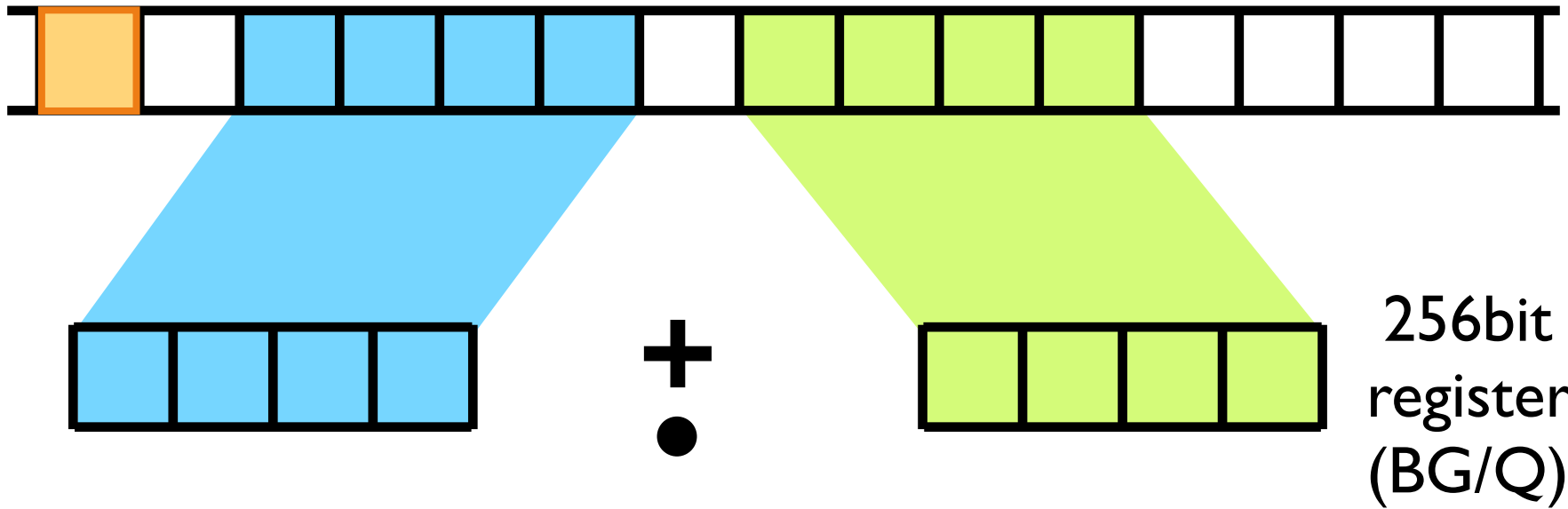




Vectorisation

double precision
floating point number (64bit)

memory





Vectorisation: initial version:

```
1  real :: rho, rho_x, rho_y, rho_z, u, v, w, rhs
2  do e=1,num_elem ! loop through all elements
3      do i=1,num_points_e ! loop through all points of
         the element e
4          ... ! compute derivatives rho_x, rho_y, rho_z
5          rhs = u*rho_x + v*rho_y + w*rho_z + ...
6      end do !i
7  end do !e
```

optimised for compiler vectorisation:

```
1  real, dimension(num_points_e) :: rho, rho_x, rho_y, &
2      rho_z, u, v, w, rhs
3  do e=1,num_elem ! loop through all elements
4      ... ! compute derivatives like rho_x, rho_y, rho_z
5      rhs = u*rho_x + v*rho_y + w*rho_z + ...
6  end do !e
```




Vectorisation: initial version:

```
1 real :: rho, rho_x, rho_y, rho_z, u, v, w, rhs
2 do e=1,num_elem ! loop through all elements
3   do i=1,num_points_e ! loop through all points of
4     the element e
5     ... ! compute derivatives rho_x, rho_y, rho_z
6     rhs = u*rho_x + v*rho_y + w*rho_z
7   end do !i
end do !e
```

9.4s
14.4% vector
operations

optimised for compiler vectorisation:

```
1 real, dimension(num_points_e) :: rho, rho_x, rho_y, &
2   rho_z, u, v, w, rhs
3 do e=1,num_elem ! loop through all elements
4   ... ! compute derivatives like rho_x, rho_y, rho_z
5   rhs = u*rho_x + v*rho_y + w*rho_z + rho
6 end do !e
```

2.1s
73.9% vector
operations



vector intrinsics (here for BG/Q):

```
1  real, dimension(4,4,4) :: rho, rho_x, rho_y, &
2     rho_z, u, v, w, u_x, v_y, w_z, rhs
3  !IBM* align(32, rho, rho_x, rho_y, rho_z, u, v, w,
4     u_x, v_y, w_z, rhs)
5  ! declare variables representing registers: (each
6     contains four double precision floating point
7     numbers)
8  vector(real(8)) vct_rho, vct_rhox, vct_rhoy, vct_rhoz
9  vector(real(8)) vct_u, vct_v, vct_w, vct_rhs
10 if (iand(loc(rho), z'1F') .ne. 0) stop 'rho is not
11     aligned'
12 ... ! check alignment of other variables
13 do e=1,num_elem ! loop through all elements
14     do k=1,4 ! loop over points in z-direction
15         do j=1,4 ! loop over points in y-direction
16             ... ! compute derivatives rho_x, ...
17             ! load always four floating point numbers:
18             vct_u = vec_ld(0, u(1,j,k))
19             vct_v = vec_ld(0, v(1,j,k))
20             vct_w = vec_ld(0, w(1,j,k))
```



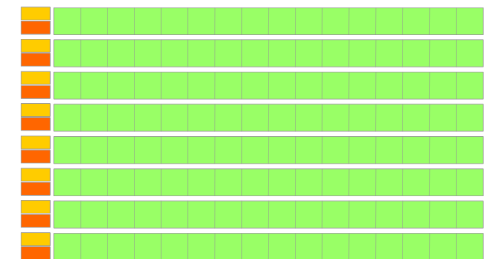
```
11      do j=1,4 ! loop over points in y-direction
12      ... ! compute derivatives rho_x, ...
13      ! load always four floating point numbers:
14      vct_u = vec_ld(0, u(1,j,k))
15      vct_v = vec_ld(0, v(1,j,k))
16      vct_w = vec_ld(0, w(1,j,k))
17      vct_rhox = vec_ld(0, rho_x(1,j,k))
18      vct_rhoy = vec_ld(0, rho_y(1,j,k))
19      vct_rhoz = vec_ld(0, rho_z(1,j,k))
20      ! rhs = u*rho_x
21      vct_rhs = vec_mul(vct_u,vct_rhox)
22      ! rhs = rhs + v*rho_y
23      vct_rhs = vec_madd(vct_v,vct_rhoy,vct_rhs)
24      ! rhs = rhs + w*rho_z
25      vct_rhs = vec_madd(vct_w,vct_rhoz,vct_rhs)
26      ! write result from register into cache:
27      call vec_st(vct_rhs, 0, rhs(1,j,k))
28      ...
29      end do !j
30      end do !k
31  end do !e
```

1.0s
98.6% vector
operations

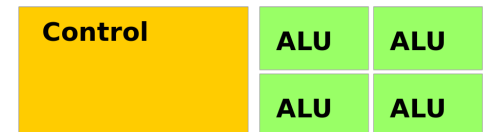


Accelerators (2 main types)

- GPU – Graphics Processing Unit
 - small number of instructions => requires host CPU
 - GPU/CPU interface (PCIe up to 16GB/sec today, in future NVLINK up to 80GB/sec between GPUs in same node)
 - more energy efficient than CPUs
 - high performance GPUs today mainly supplied by NVIDIA
 - lots of cores share one control unit
 - very little memory inside the GPU
- INTEL (Xeon Phi, aka “MIC”)
 - “Knights Corner” from 2012 requires CPU host (via PCIe)
 - “Knights Landing” from 2016, does not require CPU host (64-72 cores), 512bit register (8 double, 16 single precision numbers)
 - “Knights Hill” from 2018



GPU



CPU



List of recommendations

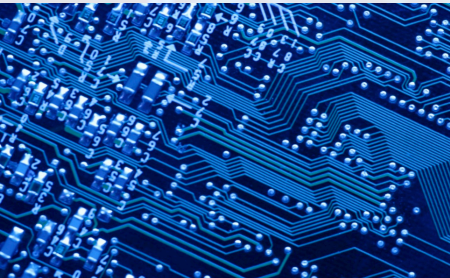
- try if using libraries is fast enough
- try to use compiler optimisation (be careful!)
- avoid unnecessary computation and communication
- decide yourself how to parallelise your code
- let the threads do work that does not affect others
- overlap computation and communication
- use data only once per time-step
- contiguous memory access
- try to fit data into cache
- **make good use of vectorisation**



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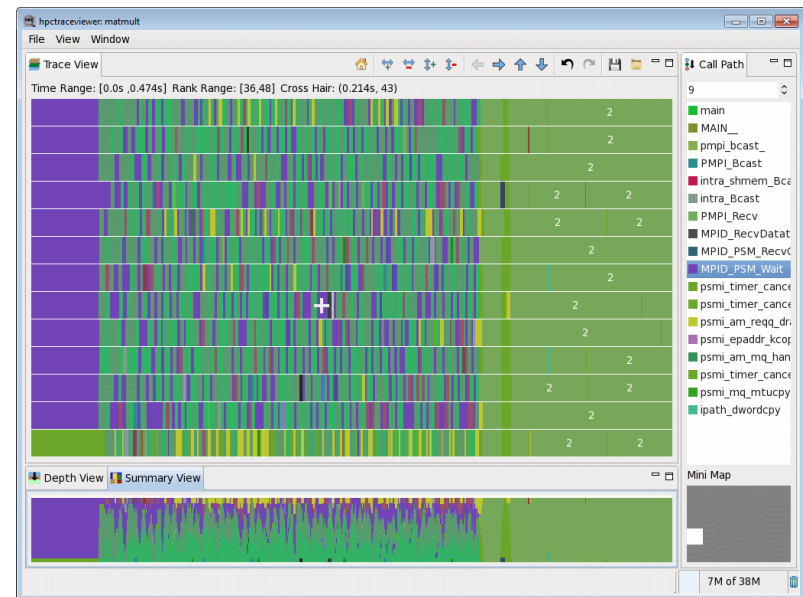
How good are we?





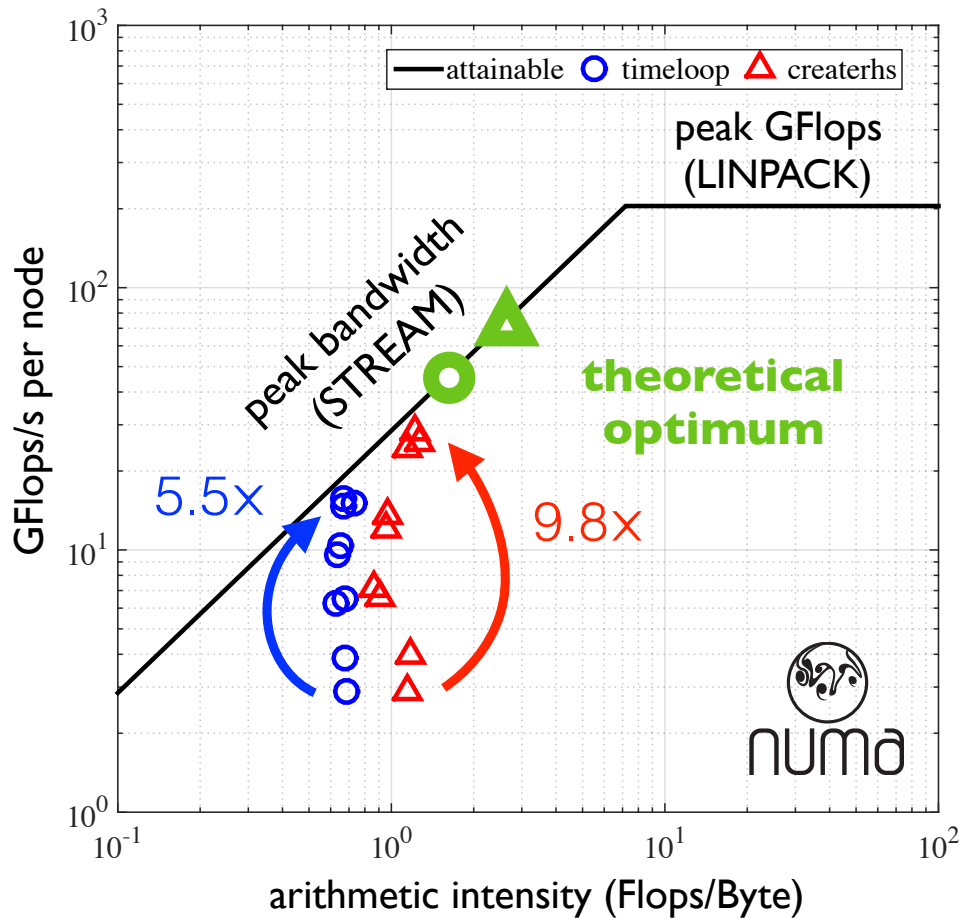
Hardware performance counters

- set of special-purpose hardware registers to store counts of hardware-related activities
- can help in spotting the application bottlenecks
- allow for low-level performance analysis and tuning, though implementation may be somehow difficult
- tools: PAPI, VTUNE, HPCToolkit, ...





Roofline plot



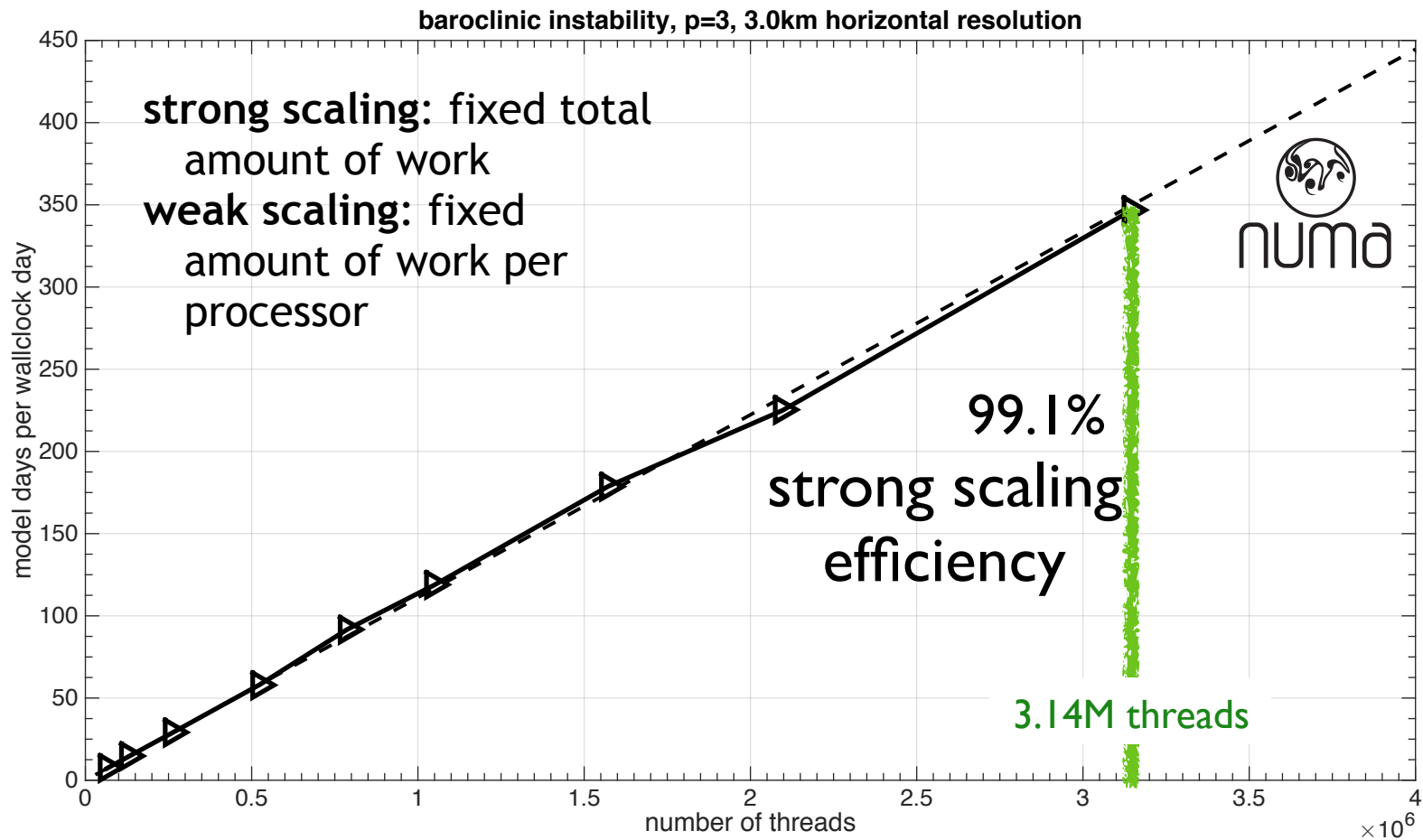
blue:
entire
timeloop

red: main
computational
kernel

data points:
different
optimization
stages



Strong scaling efficiency





Create performance model

example code:

```

real, dimension(N,M) :: a,b,c
integer :: i,j,N,M
do timestep=1,nstep
  do j=1,M
    do i=1,N
      a(i,j) = a(i,j) + b(i,j) * c(i,j)
    end do
  end do
end do
end do

```

parameters:

parameter	value
N	1E+04
M	1E+05
nstep	100
GB/s	20
GFlops/s	200

floating point operations:

function	operations per step	
main	2*N*M	2E+11
total GFlops for all steps		20000
runtime		100.0

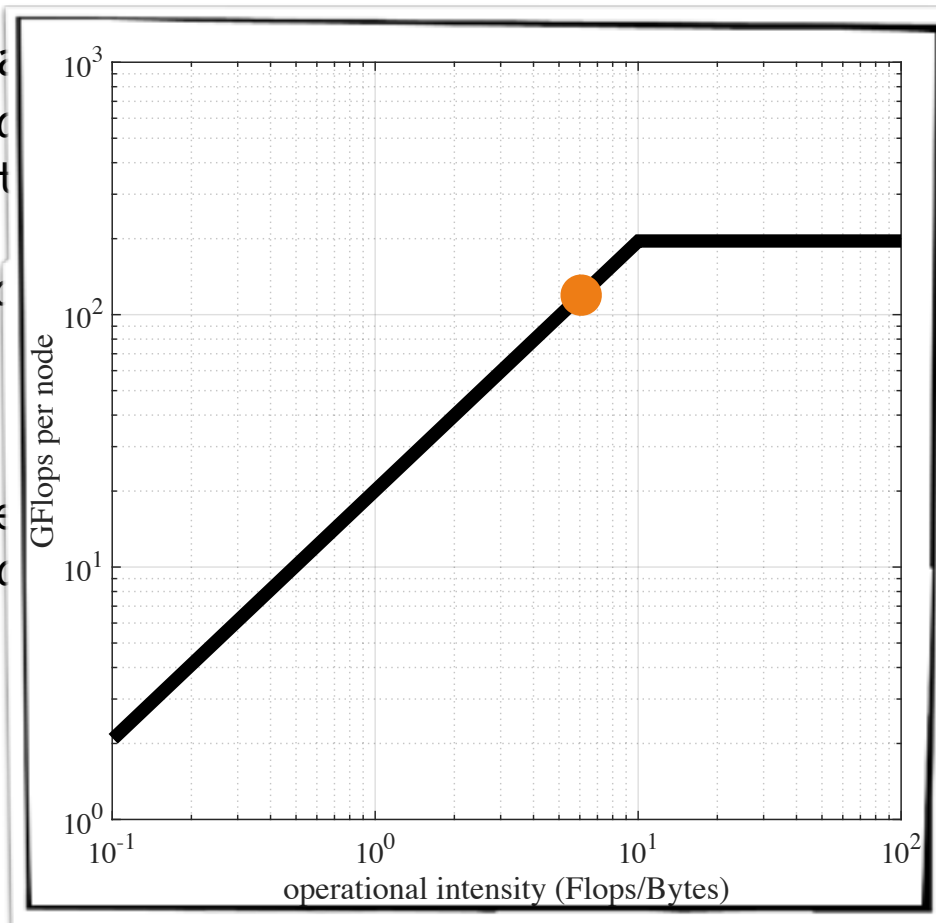
memory:

variable	bits per entry	size	#read per step	#write per step	total bits read	total bits written
a	64	N*M	1	1	6.4E+12	6.4E+12
b	64	N*M	1	0	6.4E+12	0E+00
c	64	N*M	1	0	6.4E+12	0E+00
sum in bits					1.92E+13	6.4E+12
sum in GB					2400	800
intensity	6.25			runtime in seconds		160.0



Create performance model

ex
rec
int
do
C
e
enc



intensity 6.25

parameters:

parameter	value
N	1E+04
M	1E+05
nstep	100
GB/s	20
GFlops/s	200

floating point operations:

function	operations per step	
main	2*N*M	2E+11
total GFlops for all steps		20000
runtime		100.0

size	#read per step	#write per step	total bits read	total bits written
N*M	1	1	6.4E+12	6.4E+12
N*M	1	0	6.4E+12	0E+00
N*M	1	0	6.4E+12	0E+00
			1.92E+13	6.4E+12
			2400	800
		runtime in seconds		160.0



Create performance model

example code:

```

real, dimension(N,M) :: a,b,c
integer :: i,j,N,M
do timestep=1,nstep
  do j=1,M
    do i=1,N
      a(i,j) = a(i,j) + b(i,j) * c(i,j)
    end do
  end do
end do
end do

```

next step: distinguish between worst case (all data has to be loaded from memory) and best case (previously used data is still in cache)

parameters:

parameter	value
N	1E+04
M	1E+05
nstep	100
GB/s	20
GFlops/s	200

floating point operations:

function	operations per step	
main	2*N*M	2E+11
total GFlops for all steps		20000
runtime		100.0

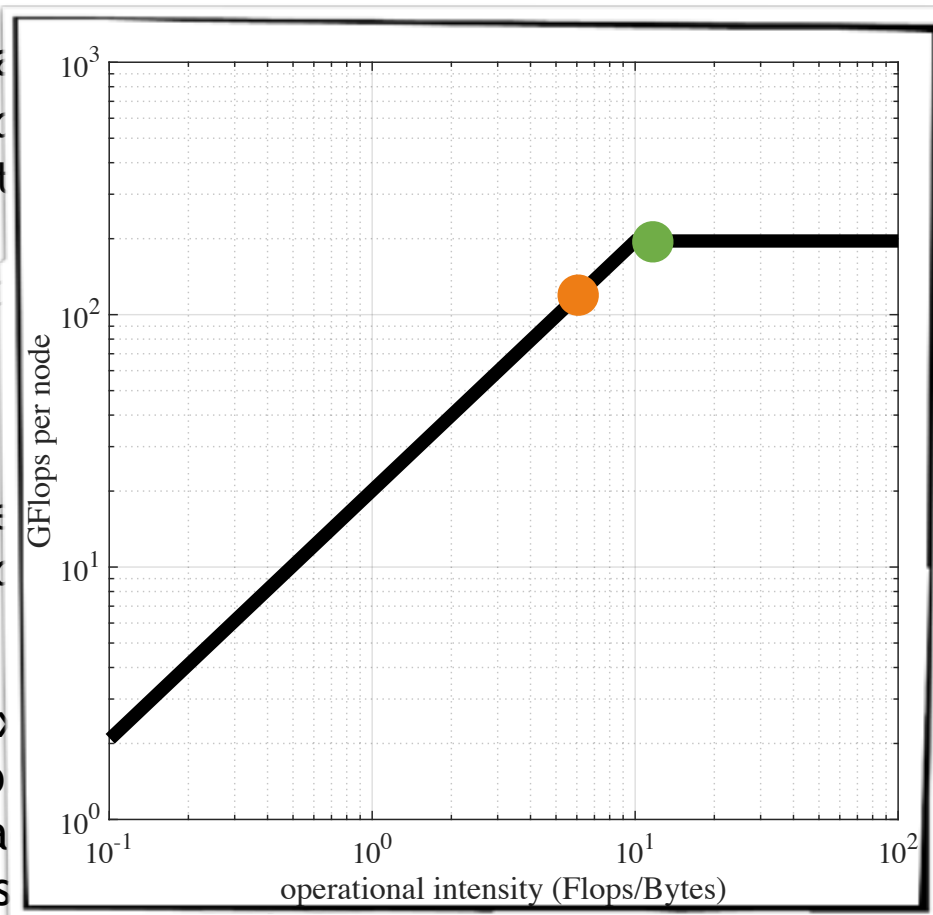
memory:

variable	bits per entry	size	#read per step	#write per step	total bits read	total bits written
a	64	N*M	1	1	6.4E+12	6.4E+12
b	64	N*M	0	0	0E+00	0E+00
c	64	N*M	0	0	0E+00	0E+00
sum in bits					6.4E+12	6.4E+12
sum in GB					800	800
intensity	12.5			runtime in seconds		80.0



Create performance model

exa
rec
int
do
C
e
enc
ne)
wo
loa
cas
still in cache)



intensity 12.5

parameters:

parameter	value
N	1E+04
M	1E+05
nstep	100
GB/s	20
GFlops/s	200

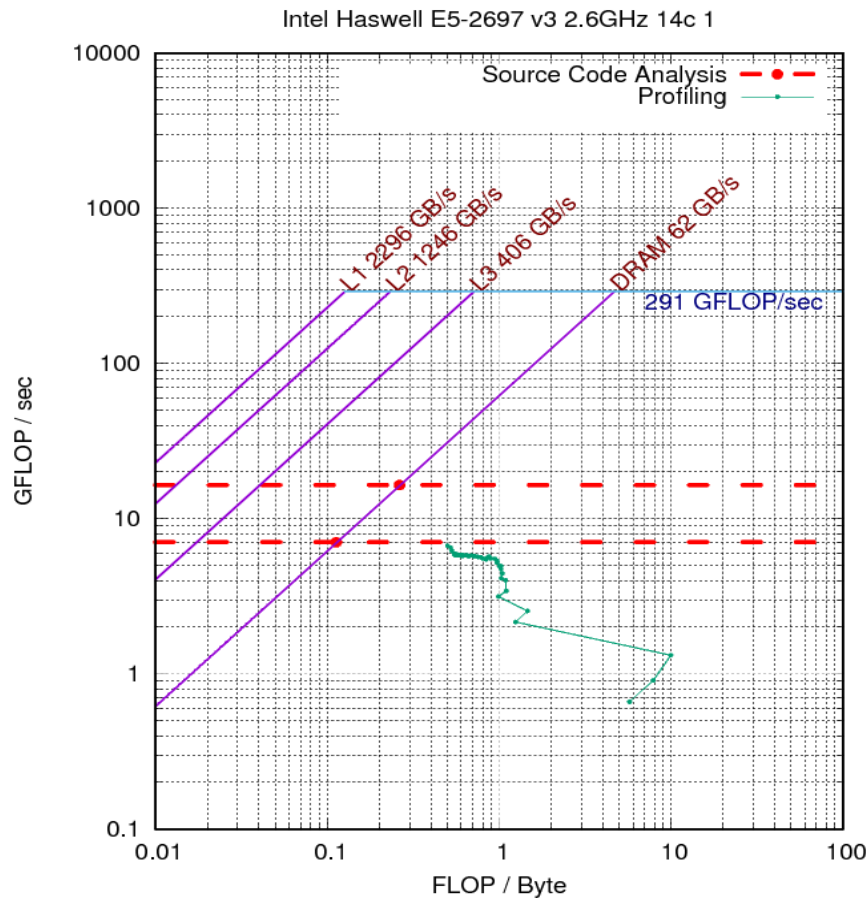
floating point operations:

function	operations per step	
main	2*N*M	2E+11
total GFlops for all steps		20000
runtime		100.0

size	#read per step	#write per step	total bits read	total bits written
N*M	1	1	6.4E+12	6.4E+12
N*M	0	0	0E+00	0E+00
N*M	0	0	0E+00	0E+00
			6.4E+12	6.4E+12
			800	800
		runtime in seconds		80.0



Roofline model



measurements and analysis performed by PSNC for spectral transform dwarf



List of recommendations

- try if using libraries is fast enough
- try to use compiler optimisation (be careful!)
- avoid unnecessary computation and communication
- decide yourself how to parallelise your code
- let the threads do work that does not affect other threads
- overlap computation and communication
- use data only once per time-step
- contiguous memory access
- try to fit data into cache
- make good use of vectorisation
- **measure performance and compare with expectations**

open question

How to find right
compromise between
performance and readability,
portability, maintainability?